

Micro and Nano Technologies

**NUMERICAL MODELING
OF NANOPARTICLE
TRANSPORT IN POROUS
MEDIA**

MATLAB/PYTHON Approach

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